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A Bayesian multidimensional IRT approach for the analysis of residents' perceptions toward tourism

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In this study, a Bayesian multidimensional item response theory (IRT) model assuming the presence of correlated general and specific latent traits is proposed for the investigation of residents' perceptions toward the tourism industry. Data collected in 2012 in the Italian Romagna area were used to study the perceived benefits and costs related to tourism. By using posterior predictive model checks and Bayesian deviance, the additive IRT model was found to fit the data well. More importantly, the results could be interpreted meaningfully, showing the most and least important perceived advantages and disadvantages of tourism for the local community. Finally, thanks to the compensatory structure of the model, the different influence of the overall attitude and the specific perceptions of the respondents could be investigated for each aspect included in the questionnaire.

keywords: Item response theory, Bayesian multidimensional models, tourism attitudes, residents' perceptions.

1 Introduction

In the last decades, the analysis of the perception and attitude of residents toward tourism development has become crucial for local governments, policymakers, and businesses because the success and sustainability of any development depends on the active support of the local populations. The investigation of the factors that influence the

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perceived impact and subsequent support for development has received an increasing attention among academics and practitioners (Deery and Jago, 2012).

In this context, the most popular theoretical framework is the social exchange theory (SET). If locals perceive that the benefits are larger than the costs, then they are inclined to be involved in the exchange and, thus, endorse future development in their community. Several empirical analyses have identified many factors influencing the reactions toward tourism: economic/social/cultural benefits, economic/social/cultural costs, the state of the local economy, the level of community concern, and the community's attachment, among others (Gursoy and Rutherford, 2004; Gursoy et al., 2009; Vargas-Sánchez et al., 2009).

As emphasized by Deery and Jago (2012), recent quantitative research in this area has not provided in-depth insight into the residents' perceptions. In particular, the need of understanding how heterogeneous are the perceptions of tourism among individuals within the same community has started to represent a major policy goal, supporting management strategies that can be put in place. In this study, we try to fill this gap using a new methodological framework based on item response theory (IRT), an approach that was originally developed in the educational field (Hambleton et al., 1991; Lord and Novick, 1968) and recently applied to the analysis of residents' support to tourism (Bernini et al., 2015). IRT moves the focus from the covariance structure analysis that is typical of structural equation models (SEM) to person-level analysis by assigning a score measuring the latent traits of each subject. In particular, following Bernini et al. (2015), we suggest using the SET approach where the perceptions of benefits and costs should be considered as latent constructs. Additionally, a general attitude toward tourism should be considered to explain the variability due to the contrast between benefit and cost perceptions.

In this paper, given the complex structure of the analyzed phenomenon, we propose the use of a multidimensional approach. The attention has only recently been devoted to models that include more than one latent trait, the so-called multidimensional IRT (MIRT) models (see, e.g., Reckase, 2009). These models perform better than separate unidimensional models in fitting the sub-groups of items regarding benefits and costs because they are able to describe the data complexity, taking into account correlated latent traits and also the hierarchical structure of the data. In particular, we introduce an additive model for dealing with items that assess several related domains that are hypothesized to comprise a general structure. Additive models are potentially applicable when there are a general factor and multiple domain specific factors, each of which is hypothesized to account for the unique influence of the specific domain over the general factor (Chen et al., 2006). In this paper, in addition to two specific traits measuring perceptions on benefits and costs of tourism, we introduce a general trait measuring an overall attitude toward tourism. Moreover, we allow all the latent variables to be correlated (Sheng and Wickle, 2007, 2009). The estimated model involves a new interpretation of item parameters and individual scores in an unusual setting, different from the most common educational one (Matteucci and Mignani, 2015). A further innovative and important aspect of our proposal deals with the estimation procedure. We applied Markov chain Monte Carlo (MCMC) methods, in a fully Bayesian framework. This approach

has the advantage of estimating item parameters and individual latent traits jointly and it is proved to be more accurate and efficient in parameter estimation compared with the usual marginal maximum likelihood (MML) method (Albert, 1992). Another possible estimation method is conditional maximum likelihood (CML) which relies on the sufficiency property and can be used for IRT models in the Rasch family (for an interesting comparison among MML and CML for multidimensional versus unidimensional models see Bartolucci (2007)).

MCMC is powerful for complicated models where the probabilities or expectations are intractable by analytical methods or other numerical approximation. Furthermore, at the end of the analysis, the user has access to the entire posterior distribution of every parameter, not just to a point estimate and standard error. Another important advantage concerns the model comparison that can be carried out using Bayes factors, Bayesian deviance and a Bayesian predictive approach, i.e. posterior predictive model checks. These model comparison techniques provide an alternative method of checking model assumptions (Sinharay et al., 2006). Among the MCMC methods, the Gibbs sampler (Geman and Geman, 1984) has been successfully applied to estimation of IRT models (see, e.g., Albert, 1992; Béguin and Glas, 2001; Edwards, 2010). The method is straightforward to implement when each full conditional distribution is a known distribution that is easy to sample from.

In this paper we refer to the estimation procedure developed by Sheng and Wikle (2008, 2009). We should provide useful insights to encourage a diffuse use of a) multidimensional models with complex latent trait structures, and b) Bayesian estimation via MCMC, among practitioners. In fact, MCMC offers the many above mentioned advantages including, from a practical point of view, a relative ease of implementation and the availability of free software. Unfortunately, the method is not largely used, probably due to the computational intensiveness that limited its use in the past.

For the case study, we consider a novel sample of residents in the Romagna area and in the nearby State of S. Marino, a developed territory that is homogeneous in terms of economic and social standards, it has cultural heritage and is highly devoted to tourism. We analyzed the data collected in 2012 from a questionnaire with several blocks of items referring to the residents' evaluations on benefits and costs of the tourism industry. The present paper improves the study of Bernini et al. (2015) in several ways. First, the analysis is carried out on a new data set related to residents' perceptions in 2012 in order to verify the robustness of results over time. Second, the IRT approach uses a different data dichotomization to better explain the results. Last, a novel procedure based on posterior predictive model checks is implemented for verifying the model fit.

The remainder of this paper is organized as follows. In Section 2 we illustrate the data and we review multidimensional IRT models, as well as model estimation and some issues on the goodness of fit. The results for the additive IRT model are presented, interpreted and discussed in Section 3. Last, in Section 4 conclusions are addressed.

2 Materials and Methods

In this section, we first describe the data used for the analysis in terms of sample and questionnaire. Some descriptive statistics on item responses are given. Secondly, multi-dimensional IRT models are introduced starting from a confirmatory approach. Finally, the estimation method is shortly described and Bayesian methods for assessing model fit are discussed.

2.1 Data and questionnaire

In the analysis, we used data collected from residents in the Romagna area in 2012. The sampling design was based on a stratification of the provinces (Rimini, Forlì and Cesena, Ravenna, San Marino) and the demographic characteristics of the population (age and gender). A total of 814 questionnaires were obtained via telephone survey mainly. Personal interviews allow to complete the survey by guaranteeing the sample representativeness and reducing missing data (see Table 1 for some descriptives on respondents).

Table 1: Profile of respondents

		Frequency	%
Gender	Male	454	55.77
	Female	360	44.23
Age	< 25	71	8.72
	25 – 35	126	15.48
	35 – 45	130	15.97
	45 – 55	152	18.67
	55 – 65	120	14.74
	> 65	215	26.41
Labour market position	Self empl. / Manager	131	16.11
	White collar / Teacher	194	23.86
	Blue collar	54	6.64
	Other	158	19.43
	Retired	216	26.57
	Student	60	7.38

Following the literature on residents perception of tourism (Gursoy and Kendall, 2006; Gursoy and Rutherford, 2004; Vargas-Sánchez et al., 2009), the questionnaire aimed at capturing residents' evaluations with respect to the cost and benefit of the tourism industry, the degree of involvement in the tourism industry, their quality of life, and the

degree of support for future development of the tourism industry, among others. A similar survey was conducted in 2010 (Bernini et al., 2015). In the survey, five items were used to measure the perceived benefits of tourism, that are local economic and employment prospects, opportunities for cultural activities, public services and quality of life improvement. As for tourism costs, items on costs included in the questionnaire deal with the perceived impact of tourism on cost of living, crime, traffic congestion, environment damage and noise. Respondents were asked to indicate whether the aspects included in the items on benefits/costs would improve/worsen their community on a 7-point anchor scale (the scale of the items with respect to costs was inverted to eliminate reverse scoring). Data are transformed to a binary scale by using the median value as a threshold. The conversion from polytomous to binary data was motivated by the fact that several response categories were not chosen by an adequate number of respondents, and as a consequence, several item-category parameters could not be estimated accurately. Working with binary data led to a meaningful interpretation of the results. Table 2 reports the response frequencies for the items B1-B5 about the perceived benefits and items C1-C5 about the perceived costs. A positive response is defined as a response higher than the median value while a negative response is defined as a response lower or equal to the median value, meaning that positive responses overcome the median judgment for each issue, while negative responses do not. Specifically, in our data, the median value is at least 3 on a scale from 1 to 7. Because the central category 4 is interpreted as a sufficiency value and the dichotomization is done taking values higher than the median, responses recoded as 1 will always be equal or above the sufficiency judgments. Then, the probability that a good response falls among insufficient scores is negligible.

Table 2: Response frequencies for the items on benefits and costs

Item	Item description	Negative responses	Positive responses	Positive responses (%)
B1	Economic support	608	206	25.3
B2	Quality of life	540	274	33.7
B3	Public services	415	399	49.0
B4	Job opportunities	581	233	28.6
B5	Cultural activities	514	300	36.9
C1	Cost of life	499	315	38.7
C2	Crime rate	580	234	28.7
C3	Environmental damage	561	253	31.1
C4	Traffic	474	340	41.8
C5	Pollution	440	374	45.9

These descriptive statistics simply show that there is a difference in the perception of the investigated aspects for both benefits and costs.

Lastly, the Cronbach's Alpha was computed for the two subtests separately, obtaining $\alpha_1 = 0.79$ and $\alpha_2 = 0.59$ for the first and second subtest, respectively. While the subtest consisting of the items on benefits shows a pretty good internal consistency, the reliability for the items on costs is only moderate. However, we believe that, due to the short test length, the value for the Cronbach's Alpha is more than acceptable, and the need for a multidimensional analysis is confirmed.

2.2 Multidimensional confirmatory IRT models

In the framework of latent variable modeling, IRT models are used to express the probability of a given response to a categorical test item as a function of both the latent variable(s) and a set of item parameters. These models were developed under the assumption of unidimensionality, i.e. the existence of a single or at least predominant latent trait underlying the response process. However, this assumption is likely to be violated in practice because most questionnaires are explicitly designed to measure multiple aspects of a given phenomenon, or because different traits such as speediness capability are accidentally involved in the measurement process.

To allow for the presence of multiple traits, multidimensional IRT models were proposed (see, e.g., Reckase (2009)), which can be distinguished into exploratory and confirmatory models mainly. In the former case, all item responses are allowed to be related to all traits, while in the latter case each single trait is characterized through a specific item subset to represent the a priori known different test subscales. Because the test in our case study was explicitly designed to measure different latent traits, we focus here on confirmatory models only.

The presence or absence of a general trait, besides the specific traits, characterizes different types of confirmatory models. Let consider a test with k binary items divided into m subtests each containing k_v items, with $v = 1, \dots, m$, submitted to a sample of n subjects and let Y_{ij} be the response variable with $i = 1, \dots, n$ and $j = 1, \dots, k$.

Within the IRT framework, one of the simplest multidimensional approaches is formalized by the so called multi-unidimensional model

$$P(Y_{vij} = 1 | \theta_{vi}, \alpha_{vj}, \delta_{vj}) = \Phi(\alpha_{vj}\theta_{vi} - \delta_{vj}), \quad (1)$$

where the probability of a positive response to a given binary item is expressed as the cumulative normal distribution function Φ depending on the item parameters α_{vj} and δ_{vj} and the specific v -th trait θ_{vi} . In particular, α_{vj} represents the item discriminating power, i.e. the capability of the item to differentiate among individuals with different trait levels, and δ_{vj} is the threshold or difficulty parameter where an high value means that the item is likely to be answered negatively and viceversa. Given that each item is characterized by two parameters, the model is also called two-parameter multi-unidimensional model. Estimation of model (1) via Gibbs sampler was proposed by Sheng and Wikle (2007) by allowing for correlated traits also. A logistic function could be used instead of the normal one as well. In this case, a new estimation method in the classical setting based on an

approximate maximum likelihood estimator was proposed by Bartolucci and Pennoni (2007).

While model (1) admits the presence of specific traits only, the additive model (2) assumes the concurrent presence of general and specific latent traits with a compensatory structure

$$P(Y_{vij} = 1 | \theta_{0vi}, \theta_{vi}, \alpha_{0vj}, \alpha_{vj}, \delta_{vj}) = \Phi(\alpha_{0vj}\theta_{0vi} + \alpha_{vj}\theta_{vi} - \delta_{vj}), \quad (2)$$

where θ_{0vi} is the overall trait and α_{0vj} represents the discrimination parameter linking the response on item j of subtest v to the θ_{0vi} . The structure of the linear predictor is compensatory, in fact a lack in the general trait can be compensated by the specific trait and viceversa in determining the probability of a positive response. The underlying structure of model (2) comes from the traditional bi-factor model, with continuous response variables and orthogonal traits (Holzinger and Swineford, 1937). Here, the model is for categorical variables and, by following the approach of Sheng and Wikle (2009), the traits are allowed to be correlated. The additive model involves the estimation of a general α_{0vj} and a specific α_{vj} discrimination parameter and a threshold parameter δ_{vj} for each item j of subtest v . Additionally, an overall trait θ_{0vi} and m specific traits θ_{vi} are estimated for each subject i .

The general structure associated to the additive model usually produces a better fit to data with respect to other multidimensional models. In fact, it is possible to directly examine the strength of the relationship between the domain specific constructs and their associated items, as the relationship is reflected in the general discrimination parameters. Moreover, the presence of correlations among the traits allows for the investigation of the relationships among the different dimensions. The study of correlations among the traits is crucial especially for model fit assessment. Particularly, when the correlation among the dimensions is high, the underlying latent structure can be thought as unidimensional, while if the correlation is almost zero, separate unidimensional models may perform better than a multidimensional one. A particular attention should be placed in the interpretation of the results, in fact indistinguishable traits from a statistical point of view due to very high correlations does not mean that the traits cannot be interpreted separately from a cognitive point of view.

2.3 Bayesian estimation and goodness of fit

Estimation of multidimensional IRT models may be conducted by using classical MML or by simulation through MCMC within a fully Bayesian framework. The latter approach is adopted here as it was recognized as more feasible than MML estimation. The estimation procedure via Gibbs sampler (Geman and Geman, 1984) is described shortly for model (2) which can be viewed as a generalization of model (1).

The Gibbs sampler works by sampling iteratively from the conditional distribution of each variable until convergence. The first step is to treat the binary response variable Y_{vij} by introducing an independent continuous normal underlying variable $Z_{vij} \sim N(\alpha_{0vj}\theta_{0vi} + \alpha_{vj}\theta_{vi} - \delta_{vj}; 1)$ truncated by zero to the left when the response is positive,

and to the right when the response is negative. In this way, the Y_{vij} can be viewed as indicator of values of Z_{vij} .

Then, informative normal priors are used for the item parameters: $\xi_{vj} \sim N_{m+2}(\mu_{\xi_v}; \Sigma_{\xi_v})$, where $\mu_{\xi_v} = (\mu_{\alpha_{0v}}, \mu_{\alpha_v}, \mu_{\delta_v})'$ and $\Sigma_{\xi_v} = \text{diag}(\sigma_{\alpha_{0v}}^2, \sigma_{\alpha_v}^2, \sigma_{\delta_v}^2)$. Normal priors are assumed for the latent traits: $\theta_i \sim N_{m+1}(\mathbf{0}; \mathbf{R})$, where θ_i is the vector of the overall and specific traits for individual i , $\mathbf{0}$ is a $m + 1$ vector of zeros and \mathbf{R} is the variance-covariance matrix for the traits. It should be noted that, for model identification purposes, trait variances are constrained to 1, so \mathbf{R} is a constrained variance-covariance matrix, where correlations are equal to the corresponding covariances.

Given the unconstrained variance-covariance matrix for the traits Σ , the final joint posterior distribution of interest is given by

$$P(\mathbf{Z}, \boldsymbol{\theta}, \boldsymbol{\xi}, \Sigma | \mathbf{Y}) \propto f(\mathbf{Y} | \mathbf{Z}) P(\mathbf{Z} | \boldsymbol{\theta}, \boldsymbol{\xi}) P(\boldsymbol{\xi}) P(\boldsymbol{\theta} | \mathbf{R}) P(\Sigma). \quad (3)$$

Because distribution (3) is intractable, the Gibbs sampler is used to sample iteratively until convergence from the treatable conditional distributions of \mathbf{Z} , $\boldsymbol{\theta}$, $\boldsymbol{\xi}$, and Σ , given the response data \mathbf{Y} . Finally, the last step consists in transforming the variance-covariance matrix Σ into the correlation matrix \mathbf{R} . All details on the method can be found in Sheng and Wikle (2009) and Sheng (2010).

A great advantage of being in a Bayesian framework is the possibility to use Bayesian model fit techniques. In fact, while the research on goodness of fit in a frequentist approach suffers from the problem of sparse data and several computational issues, Bayesian methods allow the use of posterior predictive model checking (PPMC) which does not rely on distributional assumptions and is relatively easy to implement, given that the entire posterior distribution of all parameters of interest is obtained through MCMC. The method was firstly developed by Rubin (1984) and was later extended to include general discrepancies by Gelman et al. (1996).

The underlying idea of PPMC is to compare the observed data with replicated data generated or predicted by the model by using a number of diagnostic measures that are sensitive to model misfit. The following description of the method is general and does not refer to IRT models specifically. Let $P(\mathbf{y} | \boldsymbol{\omega})$ be the likelihood for a particular model applied to data \mathbf{y} depending on a set of parameters $\boldsymbol{\omega}$, $P(\boldsymbol{\omega})$ the prior distribution of the parameters and $P(\boldsymbol{\omega} | \mathbf{y})$ the corresponding posterior distribution. In PPMC, the distribution of interest is the posterior predictive distribution (PPD) of replicated data \mathbf{y}^{rep} , given by

$$P(\mathbf{y}^{rep} | \mathbf{y}) = \int P(\mathbf{y}^{rep} | \boldsymbol{\omega}) P(\boldsymbol{\omega} | \mathbf{y}) d\boldsymbol{\omega}. \quad (4)$$

Once chosen a discrepancy measure D , the method works by comparing the posterior distribution of $D(\mathbf{y}, \boldsymbol{\omega})$ to the posterior predictive distribution of $D(\mathbf{y}^{rep}, \boldsymbol{\omega})$, where any systematic difference means a failure of the model to explain the particular aspects of the data under investigation. Of course, the selection of an appropriate discrepancy measure is fundamental for the success of the method. Discrepancy measures should take into

account the main aspects of the model to be detected, the data features that the model is not able to consider, and the scientific purposes of the research.

In the IRT framework, it is important to check for unidimensionality or multidimensionality. In the literature, the odds ratio was proposed by Sinharay et al. (2006) as an effective measure of fit, by examining the associations between the responses to pairs of items $j, j' = 1, \dots, k$

$$OR_{jj'} = \frac{n_{11}n_{00}}{n_{10}n_{01}}, \quad (5)$$

where $n_{kk'}$ is the number of individuals scoring k on the first item and k' on the second item, with $k, k' = 0, 1$.

The results of the chosen discrepancy measure can be investigated by a graphical approach. However, it is possible to define a tail-area probability, also known as a posterior predictive p -value (PPP-value) as

$$PPP - value = P(D(\mathbf{y}^{rep}, \boldsymbol{\omega}) \geq D(\mathbf{y}, \boldsymbol{\omega}) | \mathbf{y}). \quad (6)$$

Given a number R of replications computed by the MCMC algorithm, the PPP-value can be estimated by simply using the proportion of replications for which $D(\mathbf{y}^{rep,r}, \boldsymbol{\omega}^r) > D(\mathbf{y}, \boldsymbol{\omega}^r)$, with $r = 1, \dots, R$. The PPP-values provide a measure of the degree to which observed data would be expected under the model, so values around 0.5 mean adequate fit while values close to 0 or 1 mean poor fit.

The approach of PPMC has several advantages. First of all, the method is very flexible and can be applied to all situations in which one is interested in goodness of fit. Secondly, the method does not rely on regularity conditions or asymptotic distributions, so there are no restrictions in the choice of the function for model checking. Lastly, the uncertainty is directly incorporated in the estimation by using the full posterior distribution rather than a point estimate, thanks to the Bayesian approach. However, we should be aware that the PPMC is not carrying out a classical hypothesis test so the method should be treated as a diagnostic measure to assess model strengths and weaknesses (Sinharay et al., 2006; Levy, 2011).

Finally, among methods for comparing the fit of different models, Bayes factors (Gelman et al., 2003) and the deviance information criterion (DIC), based on the posterior distribution of the deviance (Spiegelhalter et al., 1998) could be used.

3 Results

The binary response data on the 5 items on benefits (B1-B5) and the 5 items on costs (C1-C5) were used to estimate the parameters for the multi-unidimensional model and the additive model via Gibbs sampler by using the MATLAB packages IRTmu2no (Sheng, 2008) and IRTm2noHA (Sheng, 2010), respectively, with a total of 20,000 iterations and 10,000 as burn-in iterations. Conjugate normal priors were specified for the item parameters and the identity matrix was chosen as prior for the trait correlation matrix.

According to the Bayesian DIC, the additive model ($DIC=7,833.62$) should be preferred in comparison to the multi-unidimensional model ($DIC=8,301.31$). Moreover, an analysis of goodness of fit was conducted through posterior predictive model checking, in particular using the odds ratio as discrepancy measure with the number of replications equal to the effective number of MCMC iterations $R = 10,000$. Figure 1 shows, for each item pair, a graphical representation of extreme PPP-values (if any) for the multi-unidimensional model (on the left) and the additive model (on the right). In particular, the PPP-values are represented in the right lower triangle of a 10×10 matrix where the right triangle sign means a PPP-value greater than 0.995 while the left triangle sign means a PPP-value lower than 0.005.

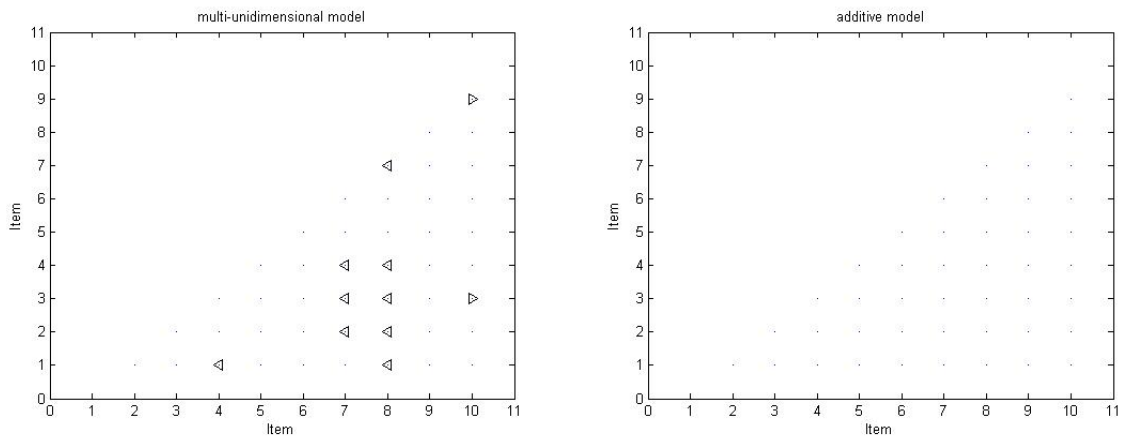


Figure 1: Graphical representation of extreme PPP-values for each item pair.

As can be clearly seen, the number of extreme PPP-values is equal to 11 for the multi-unidimensional model. Because the number of different item pairs is equal to 45, it means that about the 24.4% of the item associations shows poor fit. This percentage is not particularly high, so we cannot say the multi-unidimensional does not fit the data at all. However, as can be seen from the same plot associated to the additive model, no extreme PPP-values are observed showing good fit. Therefore, it can be concluded that the presence of an overall latent variable, besides the specific ones, assumed in the additive model is well supported by data.

Under a confirmatory approach, the additive model assumes that the item responses on benefits are related to a first trait θ_1 , the item responses on costs are related to a second trait θ_2 , and all items are directly related to a general trait. Moreover, the three traits are allowed to be correlated. According to an analogous interpretation for the traits given by Bernini et al. (2015), the specific traits can be interpreted here as specific perceptions, i.e. perception of tourism benefits and perception of tourism costs. Because the items on costs were reverse scored, high individual scores for both traits are associated with positive perceptions of the effect of the tourism industry. In particular, as the score on the first dimension increases, as the positive perception of the effect of tourism on the

local environment increases. Analogously, the higher the score on the second dimension is, the lower the perception of a negative impact of tourism on the social and natural environment. Finally, the overall trait θ_0 can be interpreted as a general attitude toward tourism, where attitude is defined as an “enduring predisposition toward places, people and behaviours” (Gu and Ryan, 2008; Deery and Jago, 2012). Our general trait can be used as a good measure of the overall attitude that is expressed by the residents toward tourism. Highest scores in the attitude are associated with individuals who perceive the highest advantages and the lowest negative impacts of tourism.

The additive model requires the estimation of a general discrimination parameter (α_{0v}), a specific discrimination parameter (α_v) and a threshold parameter (δ_v) for each item. Table 3 shows the estimates for the item parameters.

Table 3: Estimates of the item parameters for the additive model (Monte Carlo standard errors in brackets)

Item	Item description	$\hat{\alpha}_{0v}$	$\hat{\alpha}_v$	$\hat{\delta}_v$
B1	Economic support	2.21 (0.04)	0.11 (0.00)	1.65 (0.03)
B2	Quality of life	0.47 (0.03)	1.04 (0.03)	0.73 (0.01)
B3	Public services	1.12 (0.04)	1.06 (0.04)	0.09 (0.00)
B4	Job opportunities	1.73 (0.02)	0.18 (0.01)	1.18 (0.01)
B5	Cultural activities	0.31 (0.03)	1.29 (0.04)	0.61 (0.01)
C1	Cost of life	0.35 (0.01)	1.05 (0.01)	0.35 (0.00)
C2	Crime rate	1.90 (0.03)	2.41 (0.03)	0.92 (0.01)
C3	Environmental damage	1.79 (0.02)	1.93 (0.02)	0.72 (0.00)
C4	Traffic	0.74 (0.02)	1.17 (0.01)	0.25 (0.00)
C5	Pollution	0.09 (0.01)	1.05 (0.01)	0.13 (0.00)

Note: $v = 1$ for the items on benefits, $v = 2$ for the items on costs

In this particular context of application, discrimination parameters represent the capability of the items to differentiate respondents with different levels of specific perceptions or attitudes, while the threshold parameters can be interpreted as the criticality of the corresponding item (Bernini et al., 2015). Under the additive model, it is not possible to order the items on the basis of their degree of criticality or response probability univocally. However, the items can be compared by fixing either the response probability or the latent traits to specific values. By fixing the overall and the specific score at zero $\theta_0 = \theta_1 = 0$ for the items on benefits, item B1 on economic support and item B4 on job opportunities show the lowest probabilities of a positive response, because they are associated to the highest thresholds, meaning that these two aspects are the most critical. Average respondents are expected to recognize the economic support and job

opportunities as the least important advantages of the tourism industry, while the improvement in the public services (item B3) is considered the most important advantage. While economic support and job opportunities are usually perceived as great advantages of tourism, the results could have been influenced by the economic crisis of these years that affected also the touristic activities. By fixing the overall and the specific score at zero $\theta_0 = \theta_2 = 0$ for the items on costs, the crime rate (item C2) and the environmental damage (item C3) are characterized by the highest threshold parameters and, consequently, represent the most critical aspects. On the contrary, pollution (item C5) appears to have the least important impact of the tourism industry for a typical respondent. We should note that all item threshold parameters are positive while, usually, they can be both positive and negative. This means that respondents have rather severe opinions about both perceived advantages and disadvantages of tourism.

In the additive model, each dimension is weighted by the corresponding discrimination parameters in determining the probability of a positive response for each item. The compensatory structure means that a low score on the general dimension can be compensated by a high score on the specific dimension, and vice versa. According to this feature, the items can be classified into three main groups: items where the effect of the overall attitude is prevalent with respect to the specific perception (B1, B4), items where the specific perception is prevalent on the general one (B2, B5, C1, C2, C4, C5) and items where both traits show similar weights (B3, C3). Graphically, the item response surfaces can be used to represent the probability of a positive response for each item given the general and the specific trait, as shown in Figure 2.

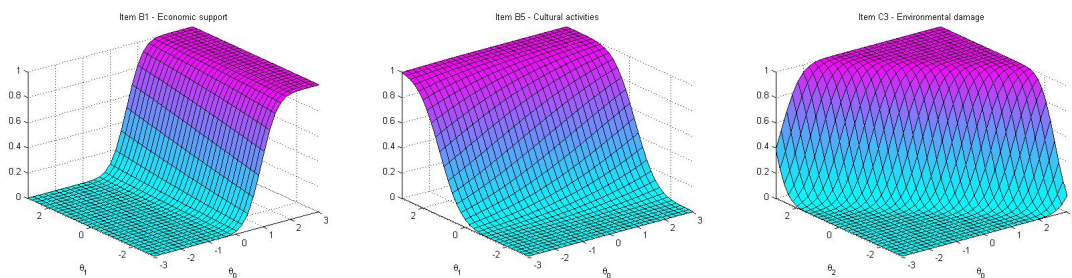


Figure 2: Item response surfaces for item B1 - Economic support, item B5 - Cultural activities, and item C3 - Environmental damage (from the left to the right)

In Figure 2, three typical items are considered. For the economic support, the probability of a positive response is almost totally influenced by the overall attitude, while the specific perception of benefits plays a marginal role. This is also true for the perceived job opportunities. Differently, responses on cultural activities are strongly determined by the specific perception instead than the general one. The same feature is observed for the quality and the cost of life, the crime rate, traffic and pollution. Finally, environmental damage is characterized by similar discrimination parameters for the two dimensions, meaning that the overall attitude and the specific perception contribute equally. A similar behavior is observed for the item on public services.

The estimates for the correlations among the trait are: $r_{01} = 0.61(0.02)$, $r_{02} = -0.84(0.00)$, and $r_{12} = -0.65(0.02)$. The correlation between the overall attitude and the perception of benefits is positive and moderate, meaning that the perception of high advantages of tourism is associated with a high and positive overall tourism attitude. On the contrary, the correlation among the overall attitude and the perception of costs is rather high and negative: high scores on the general trait are associated to low scores on the specific perception on costs, i.e. high disadvantages of tourism. The correlation among the two specific perceptions is then moderate and negative, meaning that people who perceive high advantages of tourism are also very critical about the related costs. These results confirm the findings of several studies on the support of community to tourism (see, among others, Gursoy and Kendall, 2006; Gursoy and Rutherford, 2004).

4 Concluding remarks

In this work, the additive IRT model was proposed to investigate residents' perceptions toward the tourism industry. This new approach was found to be effective in evaluating both a general attitude and the specific perceptions of the community toward tourism and showed good fit according to Bayesian DIC and PPMC. The results showed that the respondents perceived differently the proposed aspects dealing with benefits and costs related to tourism. Surprisingly, a typical respondent does not consider economic support and job opportunities as immediate advantages of tourism, while an increase in the public services is recognized as the strongest benefit. The most critical aspects are then identified in the crime rate and environmental damage. The compensatory structure of the model allowed to investigate which latent dimension was more involved in explaining the item responses. In fact, while responses on economic support and job opportunities are strongly influenced by the general attitude toward tourism and the responses on public services and environmental damage are equally influenced by both traits, most aspects proposed in the items have found to be affected by the specific perception on benefits or costs mainly. For this reason, we believe that it is very important to include in the model both kinds of latent variables and to allow them to correlate.

Future research should investigate more in detail the heterogeneity of the residents with respect to the latent dimensions identified by the model. In fact, if relevant differences are observed with respect to individual characteristics, targeted policy strategies could be suggested. The study of the differences in the scores obtained by the respondents can be done ex-post by analyzing the trait scores with respect to the individual characteristics or by including the individual covariates directly in the model. For the latter approach, multi-group IRT models (see, e.g., Azevedo et al., 2012) or IRT-MIMIC models (see, e.g., Bertaccini et al., 2013) can be used. From the methodological point of view, the sensitiveness of the results to the choice of different prior distributions should be investigated. Finally, models with different structures such as higher-order models could be studied.

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